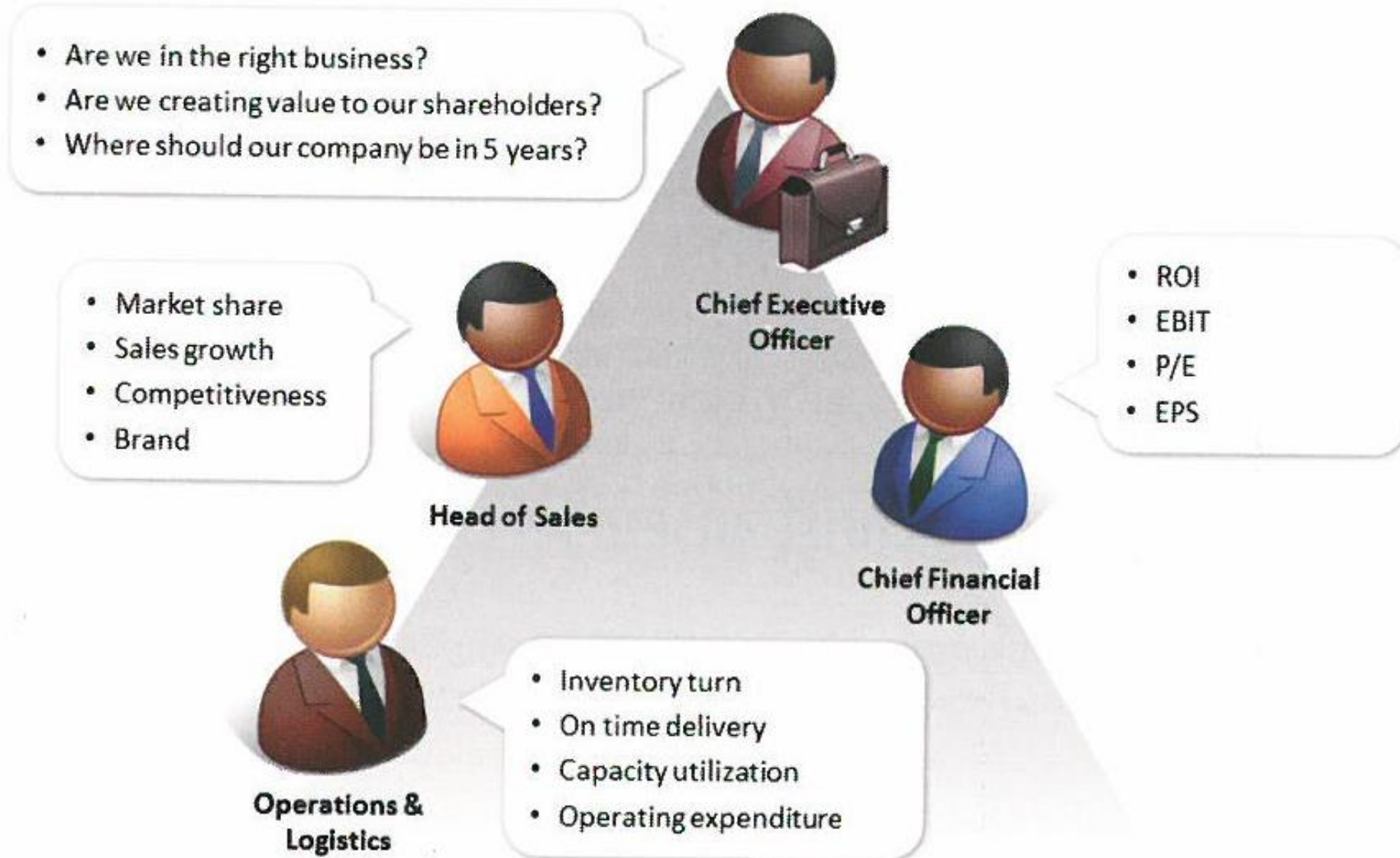


Fundamentals of Materials Management and Lot Sizing

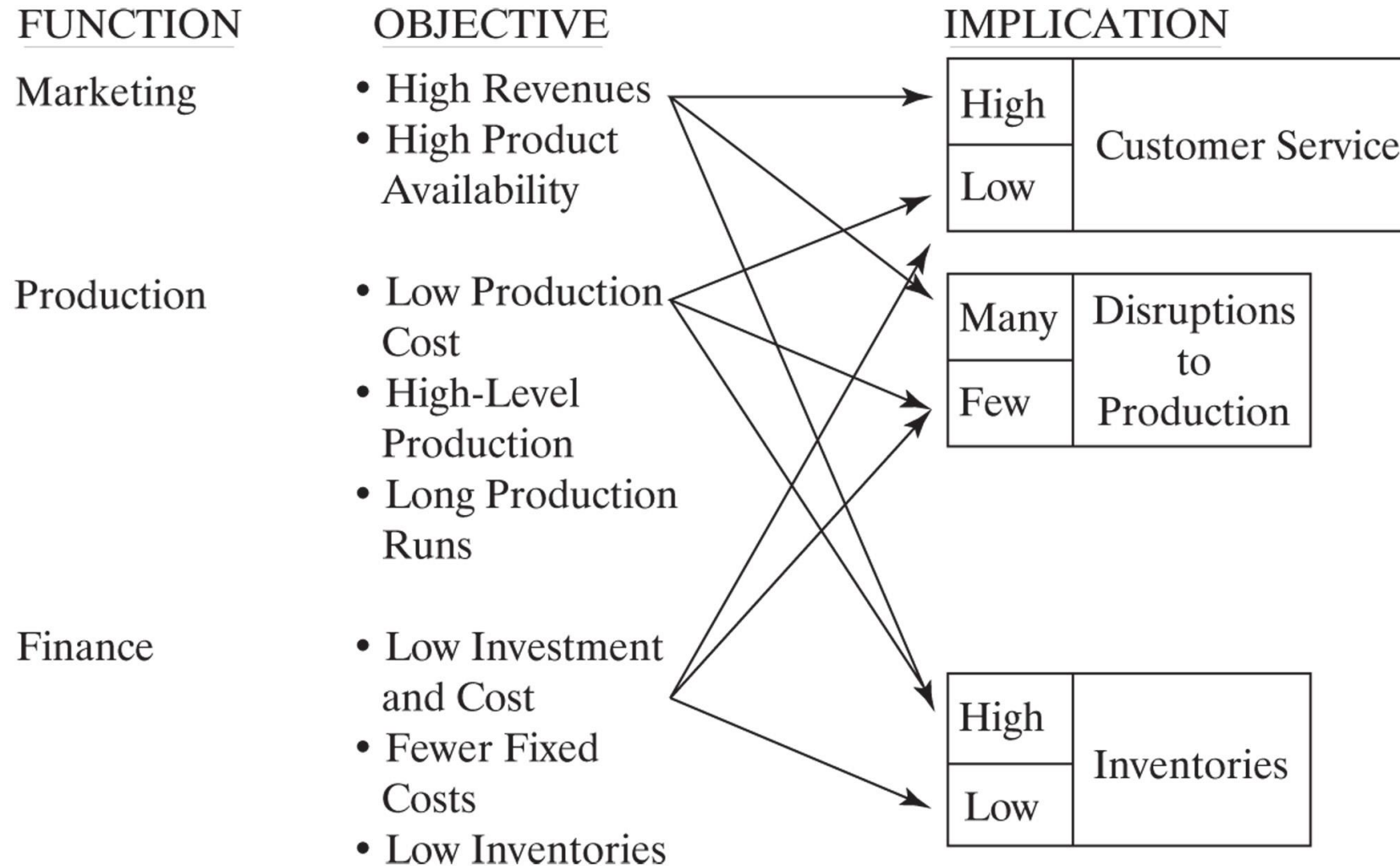
Juha Sipilä

jamk

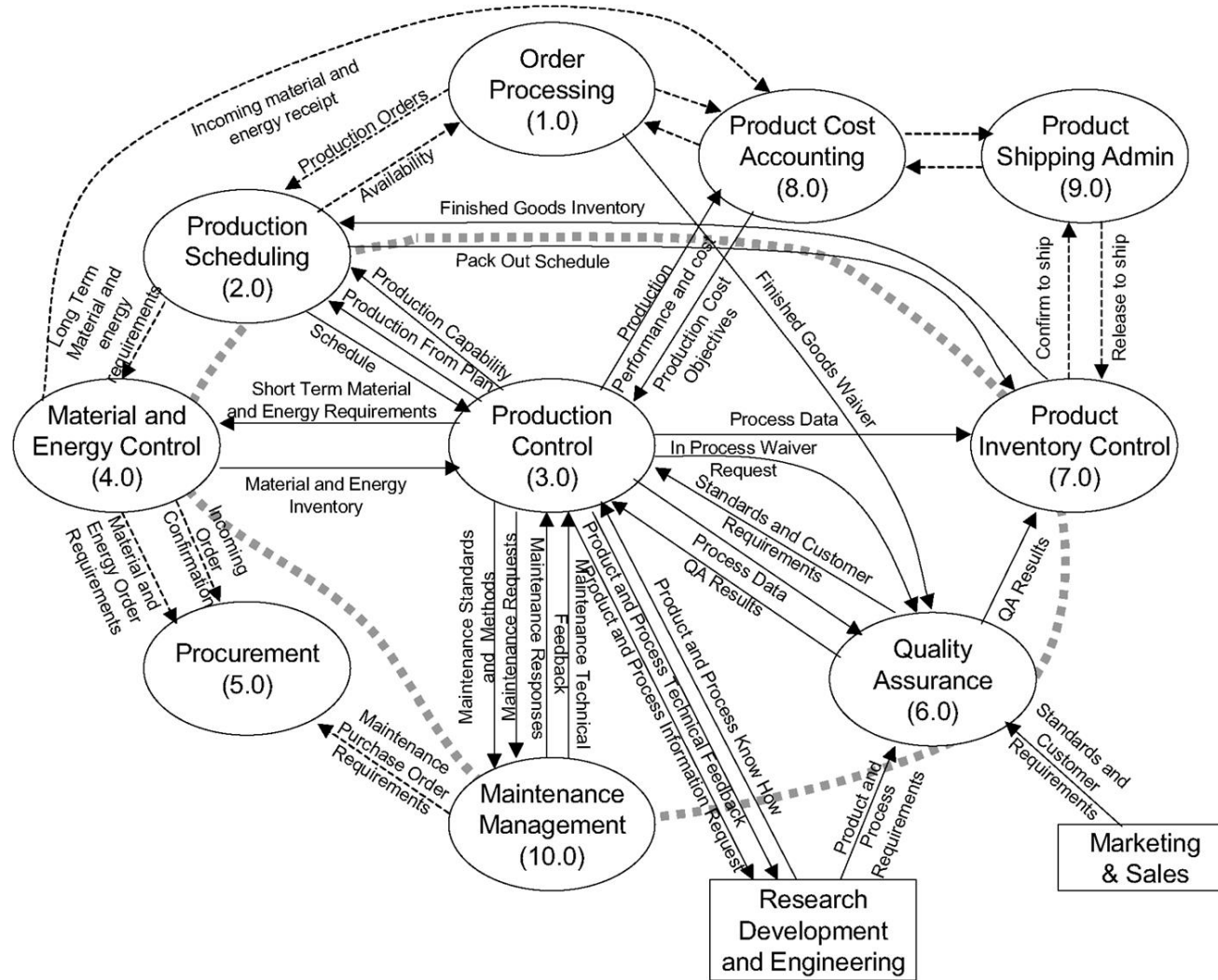
What's on top managements agenda?



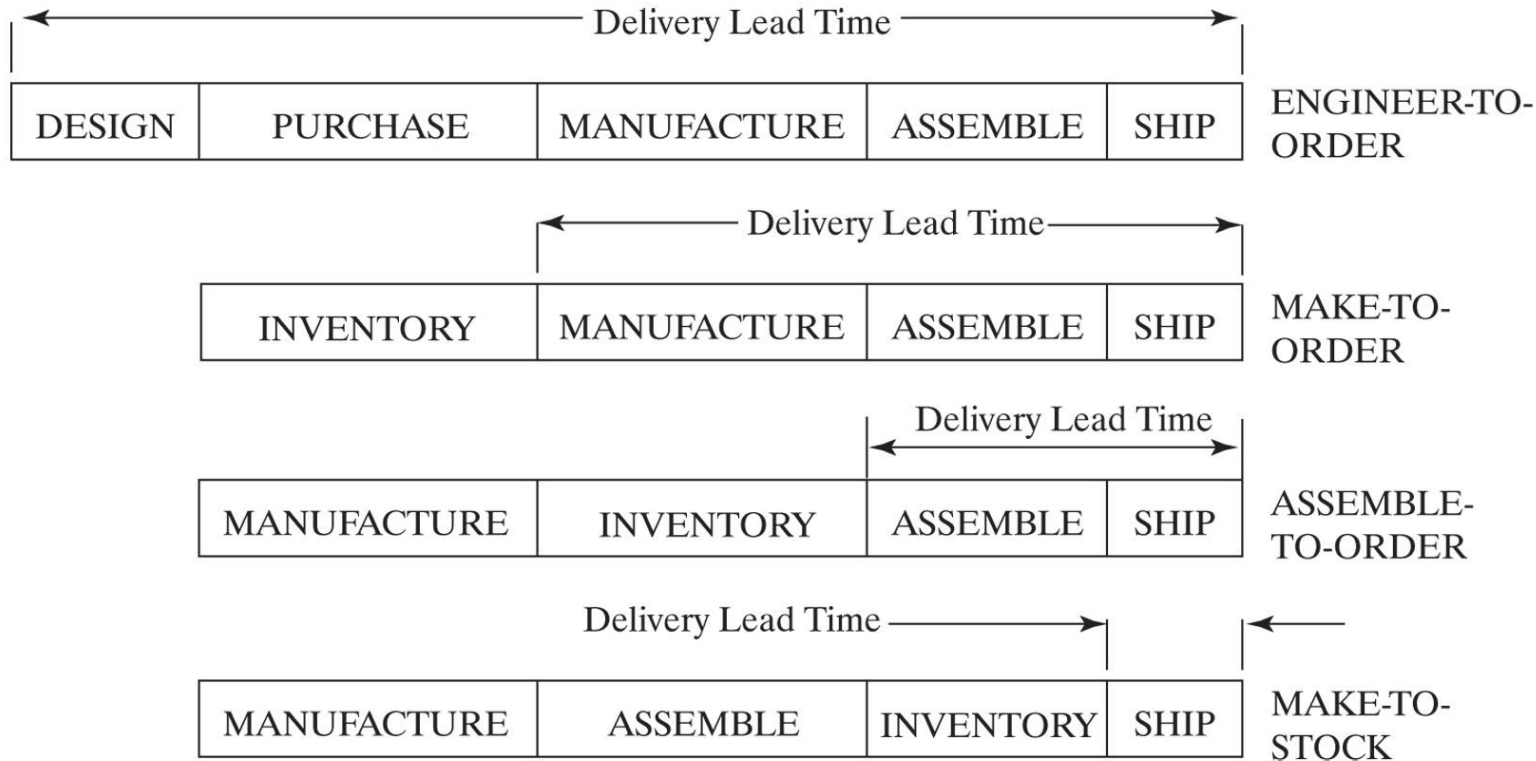
The “natural” conflict of management in production companies



ISA-95



About production strategies...



Some terms

Lead Time: how long it takes from order to delivery

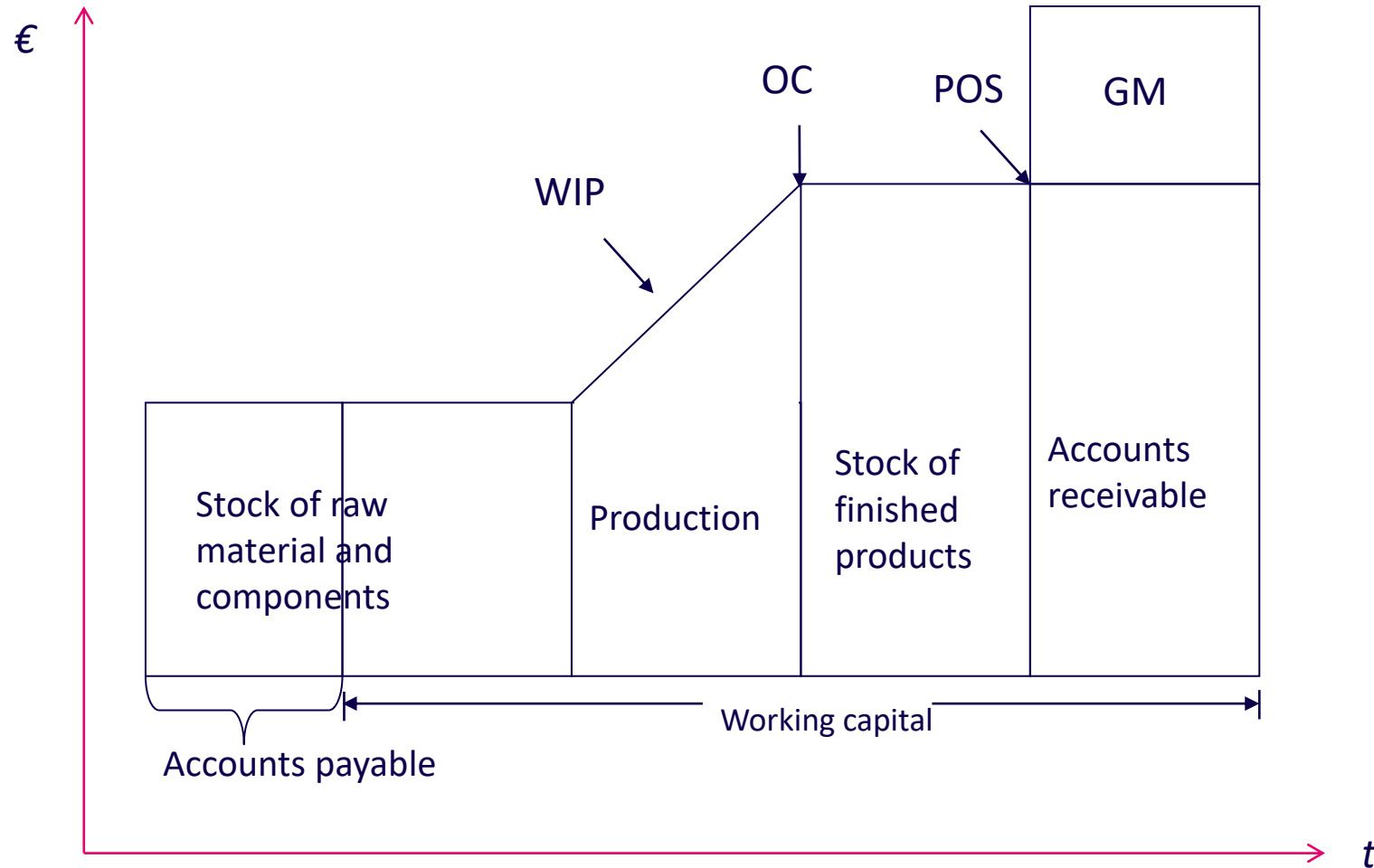
Throughput Time (TH): how long it takes to complete product from start to stock or shipment

Cycle Time or Takt Time (CT): how long are work phases in production (should be balanced)

WIP = Work in Process

Little's Law: $WIP = TH \times CT$

Schematic chart of Working Capital and WIP

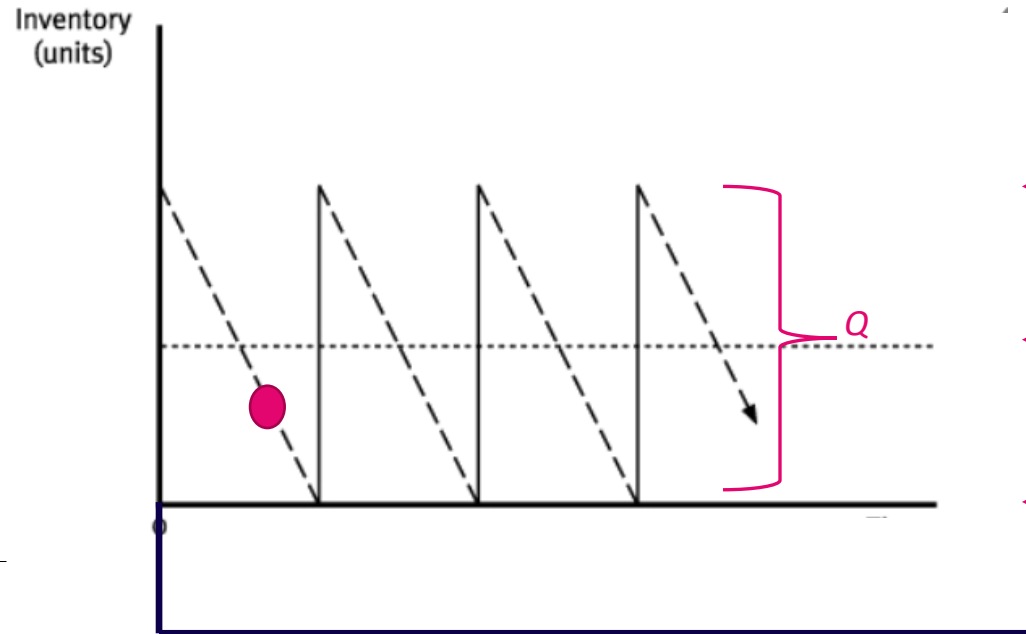


GM = gross margin
POS = Point of Sales
OC = Own Cost of product(s)

Uusi-Rauva ym. (modified)

Background for lot sizing

- Why do we have SKUs (Stock Keeping Unit)?



$Q = \text{Lot Size}$

$\text{Max inventory} = Q + SS$

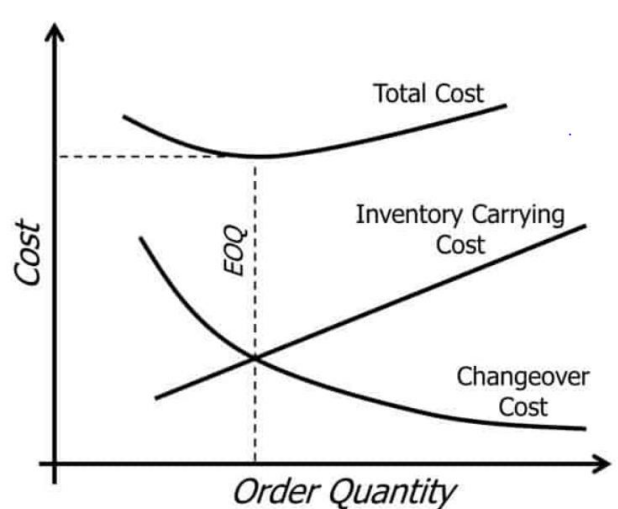
$\text{Avg inventory} = Q/2 + SS$

$\text{Safety Stock } SS \text{ (see e.g., Talluri)}$

● = Reorder Point (ROP) typically \bar{D}_L

Background for lot sizing

- **What is lot sizing?**
- The eldest known approach is *EOQ* (Economic Order Quantity) and it's "sister" formula *EPL* (Economic Production Lot)
- First introduced 1913 by Harris.
- Widely studied method, Andriolo *et al.*



$$EOQ = \sqrt{\frac{2 \times D \times S}{H}}$$

where

D = annual demand (units)

S = cost per order (or ordering costs)

I = holding cost %

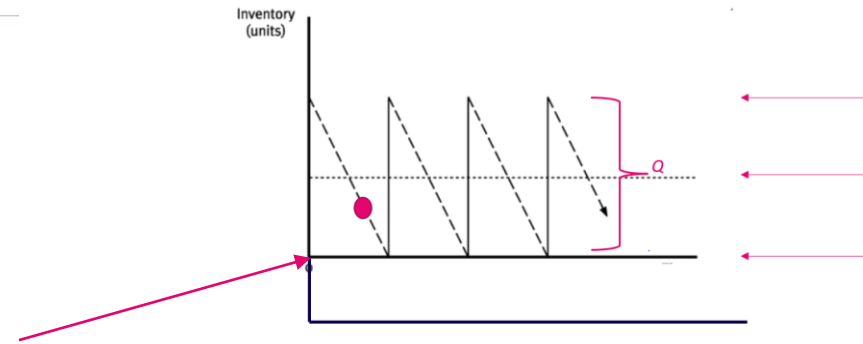
H = holding costs (€) = $I \times C$

Assumptions (Basic EOQ)

- Demand is known and independent
- Lead time is known and constant
- Receipt of inventory is instantaneous and complete
- Quantity discounts are not considered
- Only variable costs are setup/ordering and holding
- No stockouts

About safety stock (SS)

		Lead-Time	
		Constant	Variable
Demand	Constant	Case I	Case II
	Variable	Case III Current Model	Case IV Proposed Model



$Q = \text{Lot Size}$

Max inventory = $Q + SS$

Avg inventory = $Q/2 + SS$

Safety Stock SS (see e.g., Talluri)

● = Reorder Point (ROP) typically \bar{D}_L

		Lead-Time	
		Constant	Variable
Demand	Constant	No Safety Stock	$R_L = RL$ $\sigma_L = \sqrt{R^2 s_L^2}$ $SS = F_s^{-1}(CSL)\sigma_L$
	Variable	$R_L = RL$ $\sigma_L = \sqrt{\sigma_R^2 L}$ $SS = F_s^{-1}(CSL)\sigma_L$	$R_L = RL$ $\sigma_L = \sqrt{\sigma_R^2 L + R^2 s_L^2}$ $SS = F_s^{-1}(CSL)\sigma_L$

Notations vary to some extent, depending on source

Talluri et al.

About safety stock (SS)... cont.

A typical table of the standard normal function $\Phi(z)$ is provided in Figure 13.22.

<i>z</i>	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998

<i>z</i>	1.282	1.645	1.960	2.326	2.576	3.090	3.291	3.891	4.417
$\Phi(z)$.90	.95	.975	.99	.995	.999	.9995	.99995	.999995
$2[1 - \Phi(z)]$.20	.10	.05	.02	.01	.002	.001	.0001	.00001

NORMS.INV.(cell)

Service level	Factor
80,00 %	0,841621
90,00 %	1,281552
95,00 %	1,644854
98,00 %	2,053749
99,00 %	2,326348
99,50 %	2,575829
99,99 %	3,719016







About our papers

- *We have written 5 papers and published 3 papers of Lot Sizing (still to come: one submitted and one accepted waiting in queue – really long thrupt time...)*
- *In all our papers we utilize Multiobjective Optimization*
- *Professor Kaisa Miettinen, JYU supervisor*
- *Her doctoral students Adhe Kania (4 papers) and Risto Heikkinen (1 paper) are the main authors*
 - *Real-life data from a production company*
 - *Supply Chain Manager acted as the DM – Decision Making Support worked in a beautiful way*
 - *We had several DM sessions – Learning Curve could be noticed*
 - *My role merely practical point of view based on industrial experience and defining Objective Functions and Constraints*
- *We have several conflicting Objective Functions (depending on the Model):*
 - *Inventory Turnover (ITO)*
 - *Cycle Service Level (CSL)*
 - *Costs (Holding Costs, Ordering Costs and Purchasing Cost)*
 - *Probability of Product Availability (PPA)*
 - *Minimum Order Quantity (MOQ)*
- *Constraints:*
 - *Fill Rate (FR)*
 - *Order Policy with MOQ and rounding value there*
 - *Lower Bound for Decision Variables (depending on the Model)*
 - *Safety Order Time (SOT)*
 - *Safety Stock (SS)*
 - *Safety Lead Time (SLT)*

Our papers

2021

Interactive Multiobjective Optimization in Lot Sizing with Safety Stock and Safety Lead Time

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Integration of lot sizing and safety strategy placement using interactive multiobjective optimization

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2023

DESMILS: a decision support approach for multi-item lot sizing using interactive multiobjective optimization

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